

Objectives

- Use The Factor Theorem to determine factors of a polynomial
- Factor the sum and differences of two cubes

<i>Factor Theorem</i>	
Theorem	Example
For any polynomial $P(x)$, $(x-a)$ is a factor of $P(x)$ if and only if $P(a)=0$.	Because $P(1) = 1^2 - 1 = 0$, $(x-1)$ is a factor of $P(x) = x^2 - 1$.

Example 1 **Determining Whether a Linear Binomial is a Factor**

Determine whether the given binomial is a factor of the polynomial $P(x)$.

a) $(x-3); P(x) = x^2 + 2x - 3$

b) $(x+4); P(x) = 2x^4 + 8x^3 + 2x + 8$

Try it

Determine whether the given binomial is a factor of the polynomial $P(x)$.

a) $(x+2); P(x) = 4x^2 - 2x + 5$

b) $(3x-6); P(x) = 3x^4 - 6x^3 + 6x^2 + 3x - 30$

Example 2 **Factoring by Grouping..**

Factor. $x^3 + 3x^2 - 4x - 12$

Try it! Factor each expression.

a) $x^3 - 2x^2 - 9x + 18$

b) $2x^3 + x^2 + 8x + 4$

Factoring the Sum and the Difference of Two Cubes	
Method	Algebra
Sum of two cubes	$a^3 + b^3 = (a + b)(a^2 - ab + b^2)$
Difference of two cubes	$a^3 - b^3 = (a - b)(a^2 + ab + b^2)$

Example 3 **Factoring the Sum and Difference of Two Cubes**
Factor each expression.

a) $5x^4 + 40x$

b) $8y^3 - 27$

Try it! Factor each expression.

a) $8 + z^6$

b) $2x^5 - 16x^2$